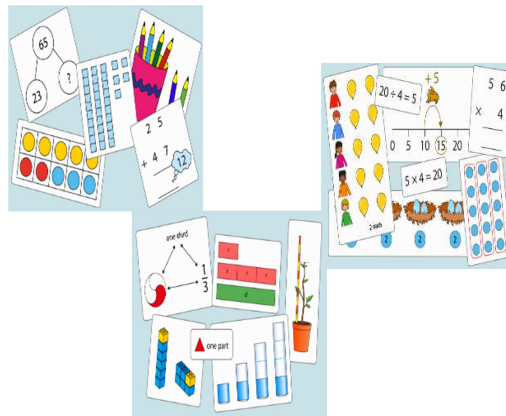




**Thurlaston CE (Aided) Primary School**  
Teaching and Living the Christian Way of Life  
Building Our Lives on Jesus

# Maths Calculation Policy

This policy shows the progression of calculation methods used from Reception to Year 6. These reflect the calculation methods introduced in our school through the National Curriculum, the NCETM Curriculum Prioritisation materials (years 1-6), and the Early Learning Goals in Reception.



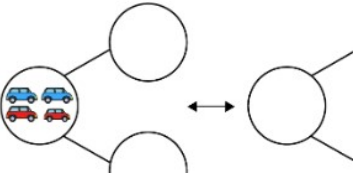



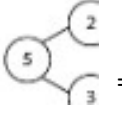

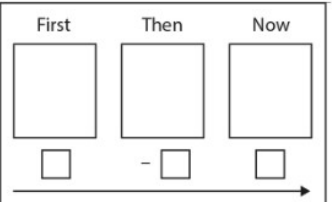

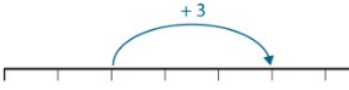
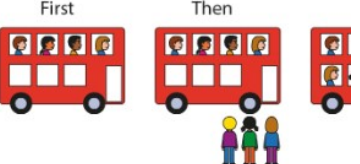
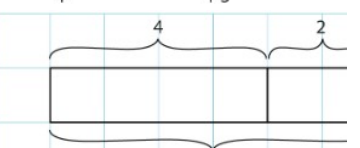
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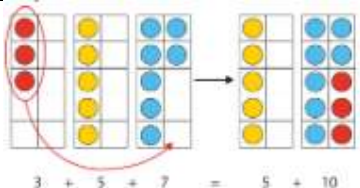

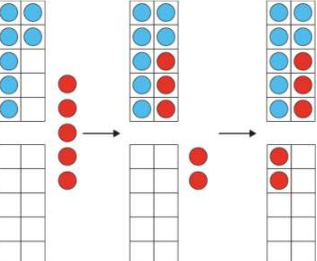
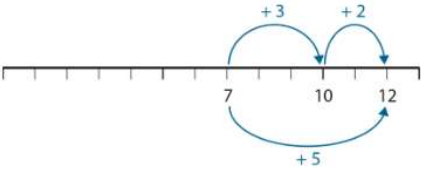
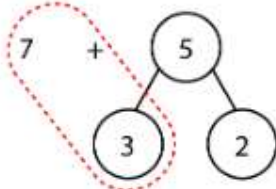
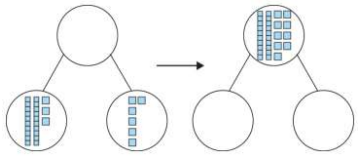
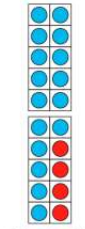
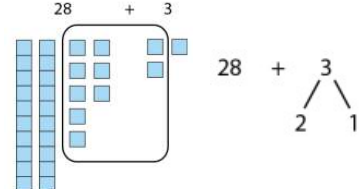
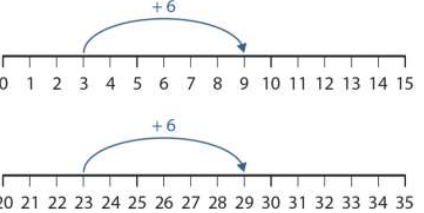
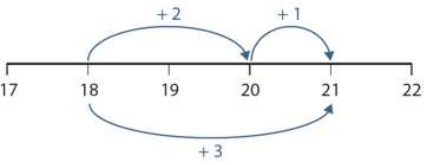
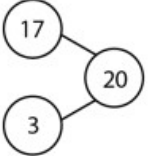
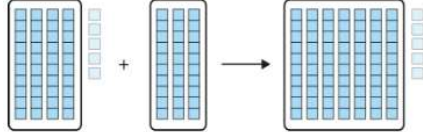
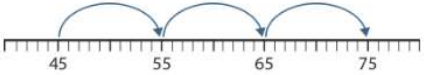
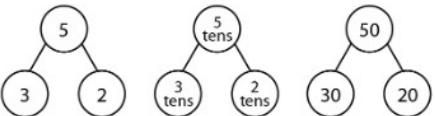
Date September 2022

Review date September 2025

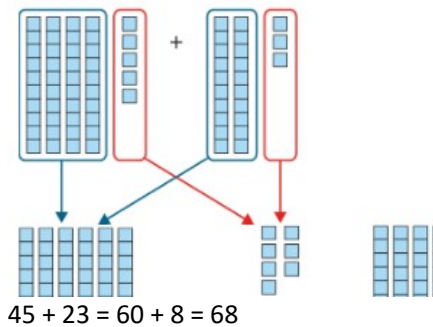


## Addition

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>___ is the whole, ___ is a part, ___ is a part.</p> <p>___ = ___ plus ___ and ___ plus ___ = ___</p> <p>There are ___ in total.</p> <p><b>Year R/1</b></p>	  $3 + 4 = 7$ $7 =$ $3 + 4$ $4 + 3 = 7$ $7 =$ $4 + 3$  $5 + 3 = 8$ $8 =$ $5 + 3$ $3 + 5 = 8$ $8 =$ $3 + 5$	 $3 + 2 = 5$ $2 +$ $3 = 5$ $5 = 3 + 2$ $5 =$ $2 + 3$	 $2 + 3 = 5$ $3 + 2$ $5 = 2 + 3$ $5 = 3$ <p>+ 2 Bar model</p> 
<p>First... Then... Now...</p> <p>e.g. <b>First</b> there were 4 children on the bus, <b>then</b> 3 children got on. <b>Now</b> there are 7 children on the bus.</p> <p><b>Year R/1</b></p>	<p>Role play getting 'on the bus' or use a toy bus.</p> 	<p>First     Then     <math>4 + 3 = 7</math></p>  $2 + 3 = 5$ 	<p>First     Then</p>   $4 + 2 = 6$

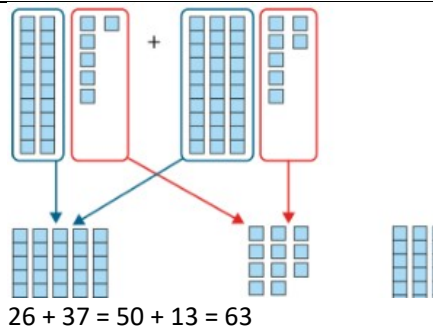
<p>We can look for pairs of addends which sum to 10.</p> <p>__ plus __ is equal to 10, then 10 plus __ is equal to __.</p> <p><b>Year 2</b></p>	 <p><math>3 + 5 + 7 = 5 + 10</math></p>		<p><math>3 + 5 + 7 = 3 + 7 + 5 = 10 + 5 = 15</math></p>
<p>First I partition the __: __ plus __ is equal to __.</p> <p>Then __ plus __ is equal to ten ... and ten plus __ is equal to __.</p> <p><b>Year 2</b></p>	 <p><math>7 + 5 =</math>  <math>7 + 3 = 10</math>  <math>10 + 2 = 12</math></p>	 <p><math>7 + 5 =</math>  <math>7 + 3 = 10</math>  <math>10 + 2 = 12</math></p>	 <p><math>7 + 3 = 10</math>  <math>10 + 2 = 12</math></p>
<p>I know that __ plus __ is equal to __. (single-digit fact)</p> <p>So __ plus __ is equal to __. (related two-digit plus single digit fact)</p> <p>I know that __ plus __ is equal to ten so __ plus __ is equal to __.</p> <p><b>Year 2</b></p>	 <p><math>3 + 6 = 9</math>  <math>23 + 6 = 29</math></p>  <p><math>16 + 4 = 20</math></p>  <p><math>28 + 3 = 31</math></p>	 <p><math>3 + 6 = 9</math></p>  <p><math>23 + 6 = 29</math></p>	 <p><math>17 + 3 = 20</math></p>
<p>I know that __ plus __ is equal to __.</p> <p>So __ tens plus __ tens is equal to __ tens.</p> <p>__ tens and __ ones, plus __ tens is equal to __ tens and __ ones.</p> <p><b>Year 2</b></p>	 <p><math>40 + 30 = 70</math> so <math>45 + 30 = 75</math></p>	 <p><math>45 + 30 = 75</math></p>	 <p><math>2 + 3 = 5</math>  <math>2 \text{ tens} + 3 \text{ tens} = 5 \text{ tens}</math>  <math>20 + 30 = 50</math></p>

First I partition the    into    and   , and the    into    and   .  
   plus    is equal to   ... (addition of the tens)  
   plus    is equal to   ... (addition of the ones)  
and    plus    is equal to   . (addition of the tens and ones)  
So    plus    is equal to   . (summary of the overall calculation)

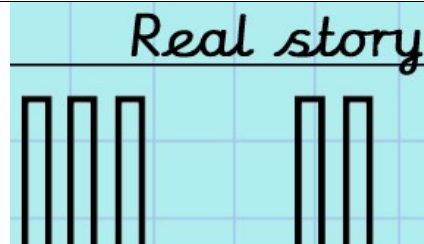


**Year 2**

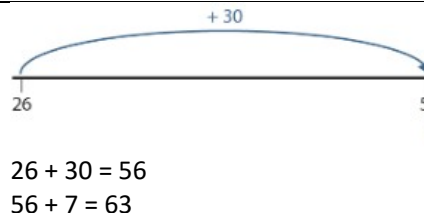
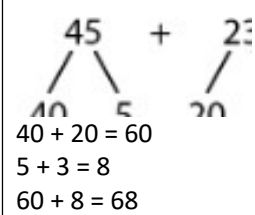
First I partition the    into    and   , and the    into    and   .  
   plus    is equal to   ... (addition of the tens)  
   plus    is equal to   ... (addition of the ones)  
and    plus    is equal to   . (addition of the tens and ones)  
So    plus    is equal to   . (summary of the overall calculation)



**Year 2**

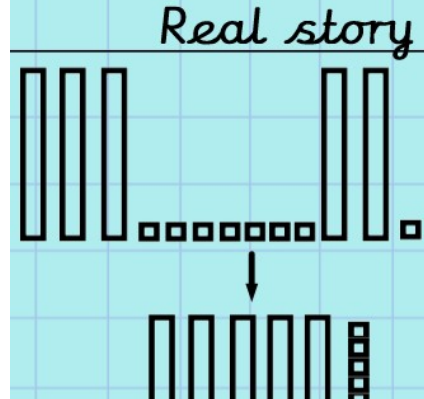


$34 + 25 =$

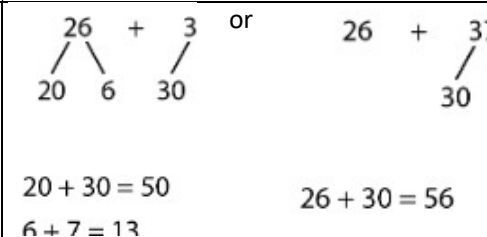


$26 + 30 = 56$

$56 + 7 = 63$



$37 + 25 = 62$



Addition Facts

Adding 1

Bonds to 10

Adding 10

Bridging/compensating

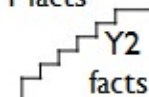
Adding 2

Adding 0

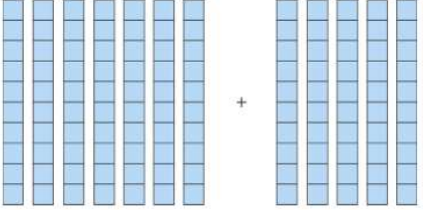
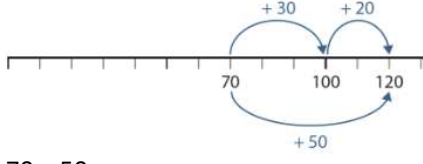
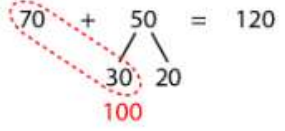
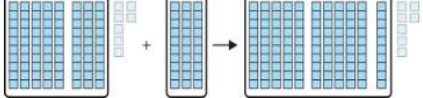
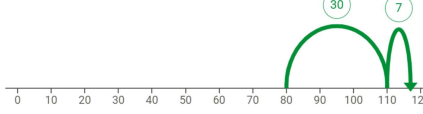
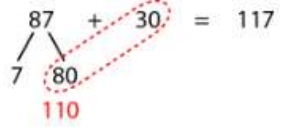
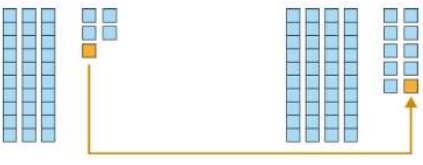
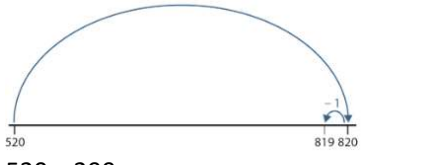
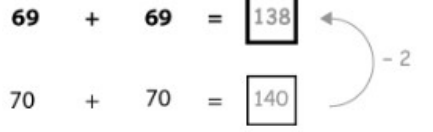
Doubles

Near doubles

Y1 facts



+	0	1	2	3	4	5	6	7	8	9	10
0	0+0	0+1	0+2	0+3	0+4	0+5	0+6	0+7	0+8	0+9	0+10
1	1+0	1+1	1+2	1+3	1+4	1+5	1+6	1+7	1+8	1+9	1+10
2	2+0	2+1	2+2	2+3	2+4	2+5	2+6	2+7	2+8	2+9	2+10
3	3+0	3+1	3+2	3+3	3+4	3+5	3+6	3+7	3+8	3+9	3+10
4	4+0	4+1	4+2	4+3	4+4	4+5	4+6	4+7	4+8	4+9	4+10
5	5+0	5+1	5+2	5+3	5+4	5+5	5+6	5+7	5+8	5+9	5+10
6	6+0	6+1	6+2	6+3	6+4	6+5	6+6	6+7	6+8	6+9	6+10
7	7+0	7+1	7+2	7+3	7+4	7+5	7+6	7+7	7+8	7+9	7+10
8	8+0	8+1	8+2	8+3	8+4	8+5	8+6	8+7	8+8	8+9	8+10
9	9+0	9+1	9+2	9+3	9+4	9+5	9+6	9+7	9+8	9+9	9+10
10	10+0	10+1	10+2	10+3	10+4	10+5	10+6	10+7	10+8	10+9	10+10

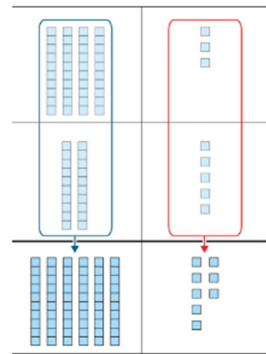
Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>I know that <u>  </u> plus <u>  </u> is equal to <u>  </u>. (single-digit addends)            So <u>  </u> tens plus <u>  </u> tens is equal to <u>  </u> tens. (multiple-of-ten addends)  <u>  </u> plus <u>  </u> is equal to one hundred and <u>  </u>.</p> <p><b>Year 3</b></p>	 <p><math>7 + 5 = 12</math>  <math>70 + 50 = 120</math></p>	 <p><math>70 + 50 =</math>  <math>70 + 30 = 100</math>  <math>100 + 20 = 120</math></p>	 <p><math>70 + 50 = 70 + 30 + 20</math>  <math>= 100 + 20</math>  <math>= 120</math></p>
<p>I know that <u>  </u> plus <u>  </u> is equal to <u>  </u>. (single-digit addends)            So <u>  </u> tens plus <u>  </u> tens is equal to <u>  </u> tens. (multiple-of-ten addends)  <u>  </u> plus <u>  </u> is equal to one hundred and <u>  </u>.</p> <p><b>Year 3</b></p>	 <p><math>87 + 30 = 110 + 7 = 117</math></p>	 <p><math>87 + 30 = 80 + 30 + 7</math>  <math>= 110 + 7</math>  <math>= 117</math></p>	 <p><math>87 + 30 = 80 + 7 + 30</math>  <math>= 110 + 7</math>  <math>= 117</math></p>
<p>First we add: <u>  </u> plus <u>  </u> is equal to <u>  </u> ...            ... then we adjust: <u>  </u> minus <u>  </u> is equal to <u>  </u>.</p> <p><b>Year 3</b></p>	 <p><math>35 + 49 = 84</math>  <math>34 + 50 = 84</math></p>	 <p><math>520 + 299 =</math>  <math>520 + 300 = 820</math>  <math>820 - 1 = 819</math></p>	 <p><math>69 + 69 = 138</math>  <math>70 + 70 = 140</math></p>

We line up the ones; \_\_\_ ones plus \_\_\_ ones.  
 We line up the tens: \_\_\_ tens plus \_\_\_ tens.  
 The \_\_\_ is in the ones column – it represents \_\_\_ ones. The \_\_\_ is in the ones column – it represents \_\_\_ ones.  
 \_\_\_ ones plus \_\_\_ ones is equal to \_\_\_ ones.  
 The \_\_\_ is in the tens column – it represents \_\_\_ tens. The \_\_\_ is in the tens column – it represents \_\_\_ tens.  
 \_\_\_ tens plus \_\_\_ tens is equal to \_\_\_ tens.

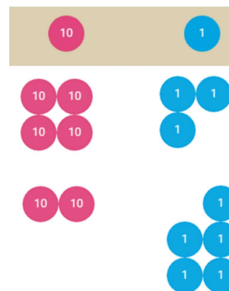
In column addition we start at the right-hand side.

**Year 3**

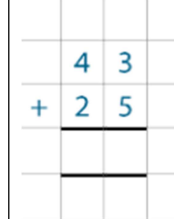
Start with two-digit numbers to exemplify lining up the columns.



Children could draw place value counters.



Start with two-digit numbers to exemplify lining up the columns.

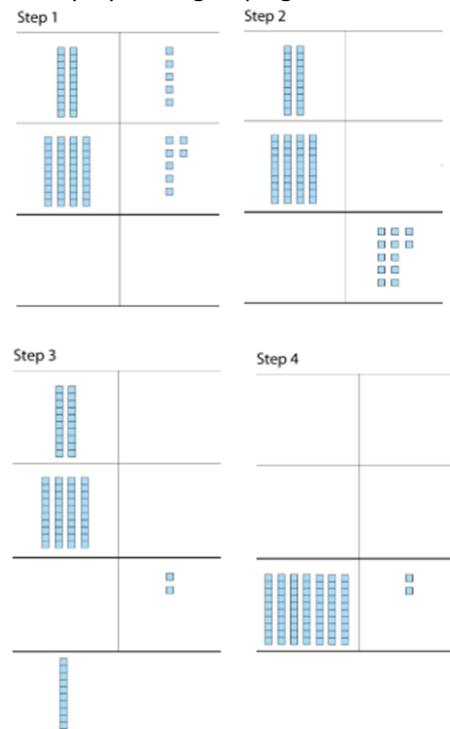


$$\begin{array}{r} 462 \\ + 205 \\ \hline \end{array}$$

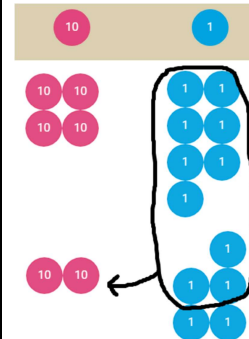
If the column sum is equal to ten or more, we must regroup.

**Year 3**

Start with two-digit numbers to exemplify the regrouping.



Children could draw place value counters.



Start with two-digit numbers to exemplify the regrouping.

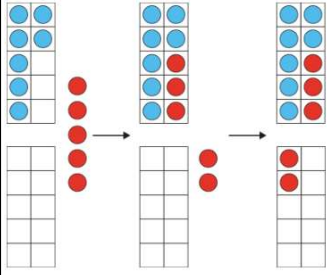
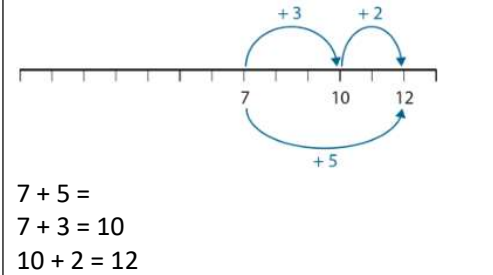
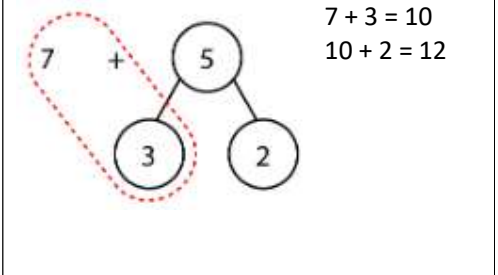
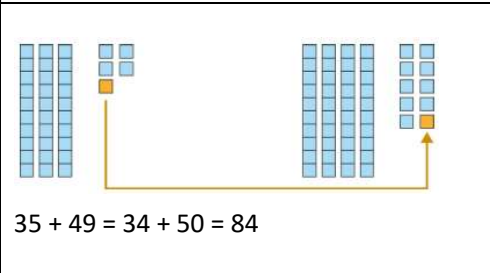
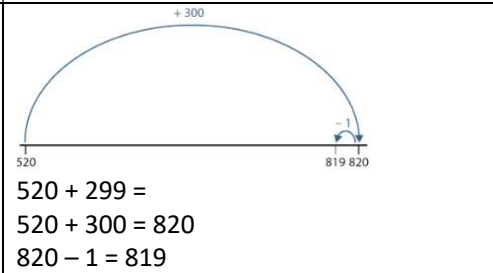
$$\begin{array}{r} 25 \\ + 47 \\ \hline 72 \end{array}$$

$$\begin{array}{r} 567 \\ + 233 \\ \hline 800 \\ 11 \end{array}$$


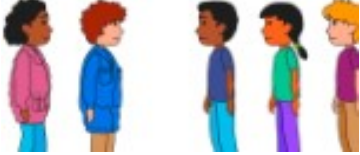
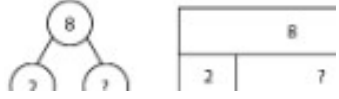
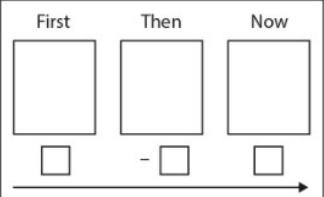
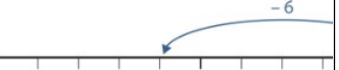
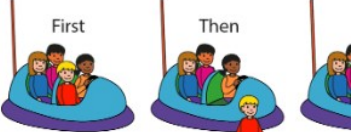
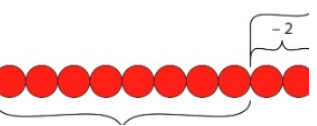
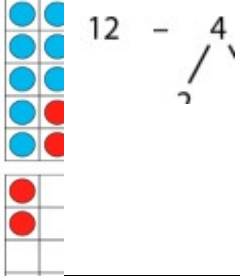
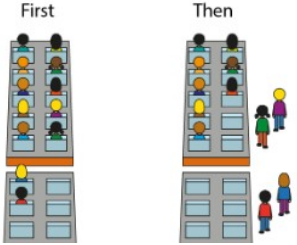
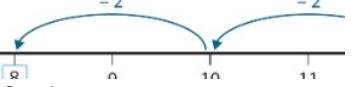
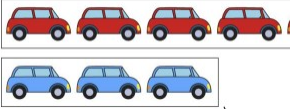
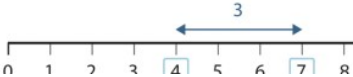
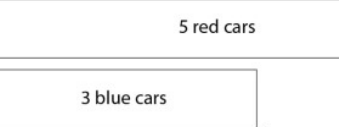


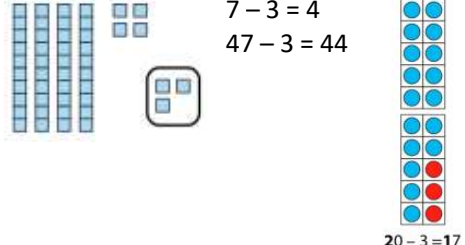
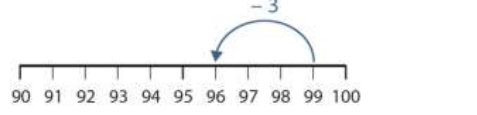
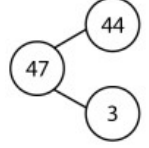
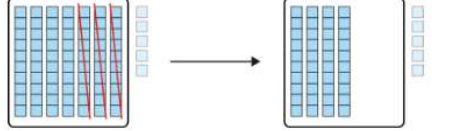
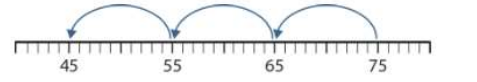
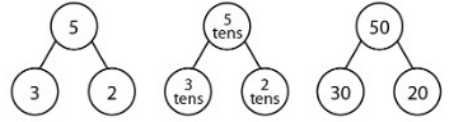
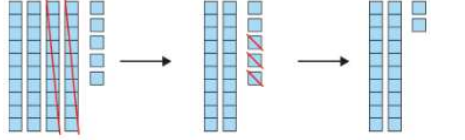
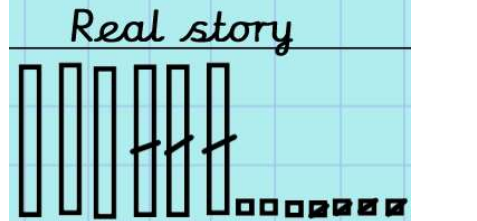
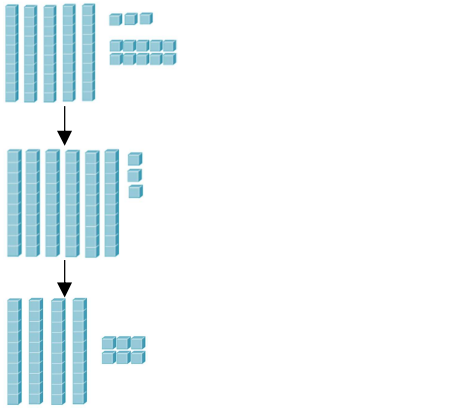

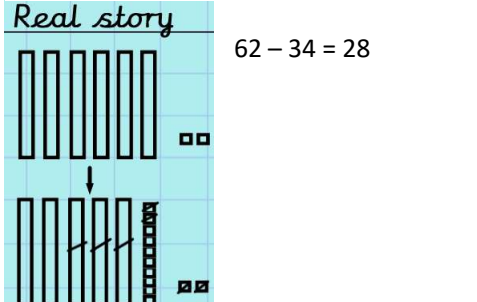
<p>If the column sum is equal to ten or more, we must regroup.</p> <p><b>Year 4</b></p>	<p>See Year 3 examples</p>	<p>See Year 3 examples</p>	$\begin{array}{r} 6,584 \\ + 2,739 \\ \hline 9,323 \\ 111 \\ \hline \pounds 24.55 \\ + \pounds 17.82 \\ \hline \pounds 42.37 \\ 11 \end{array}$
<p>If the column sum is equal to ten or more, we must regroup.</p> <p><b>Years 5 and 6</b></p>	<p>See Year 3 examples</p>	<p>See Year 3 examples</p>	<p>As in Year 4 but using numbers with more than 4 digits</p>

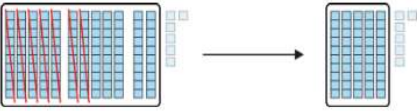
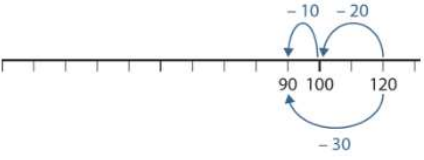
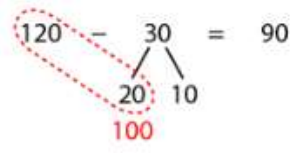
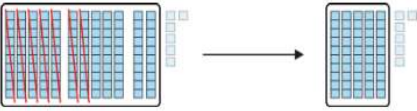
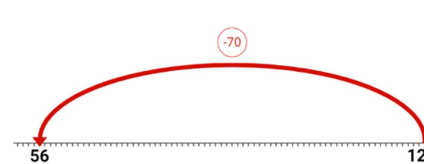
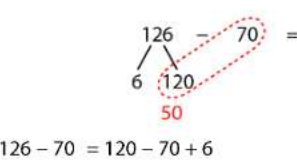
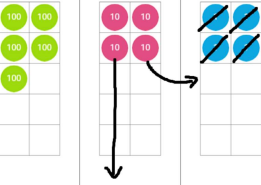
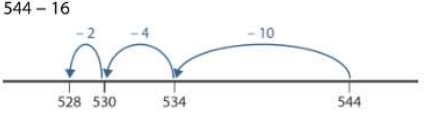
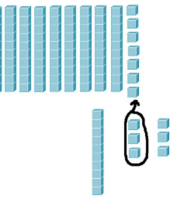
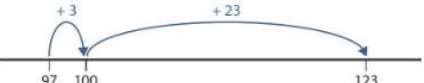
### Addition – Key mental strategies for Key Stage 2

Strategy	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>Bridging through a multiple of 10, 100, etc</p> <p><b>Years 3, 4, 5 and 6</b></p>	 <p>7 + 5 = 7 + 3 = 10 10 + 2 = 12</p>	 <p>7 + 5 = 7 + 3 = 10 10 + 2 = 12</p>	 <p>7 + 3 = 10 10 + 2 = 12</p>
<p>Compensating – rounding to the nearest multiple 10, 100, etc and adjusting</p> <p><b>Years 3, 4, 5 and 6</b></p>	 <p>35 + 49 = 34 + 50 = 84</p>	 <p>520 + 299 = 520 + 300 = 820 820 - 1 = 819</p>	<p>69 + 69 = 138</p> <p>70 + 70 = 140</p> <p style="text-align: right;">← -2</p>

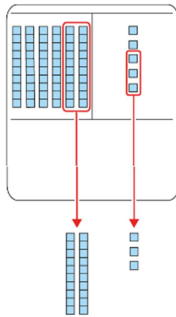
## Subtraction

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>___ is the whole, ___ is a part, ___ is a part.</p> <p>___ = ___ minus ___ and ___ minus ___ = ___</p> <p><b>Year R/1</b></p>	<p>I have 8 counters. 5 counters are red. How many are blue?</p> 	<p>There are 6 children. 2 have their coat on. How many do not have their coat on?</p> 	<p>There are 8 flowers. 2 are red and the rest are yellow. How many are yellow?</p>  $8 - 2 = 6$
<p>First... Then... Now...</p> <p>e.g. <b>First</b> there were 4 children in the car, <b>then</b> 1 child got out. <b>Now</b> there are 3 children in the car.</p> <p><b>Year R/1</b></p>	<p>Role play 'getting out of a car'.</p> 	<p>First: 4 children in a car. Then: 1 child gets out. Now: 3 children in the car.</p> <p><math>4 - 1 = 3</math> <math>3 = 4 - 1</math></p> 	 <p>4                      -1</p>
<p>We partition the ___ into ___ and ___.</p> <p>First we subtract the ___ from ___ to get to 10.</p> <p>Then we subtract the remaining ___ from 10.</p> <p>We know 10 minus ___ is equal to ___.</p> <p><b>Year 2</b></p>	 <p><math>12 - 4 =</math> <math>12 - 2 = 10</math> <math>10 - 2 = 8</math></p> 	<p>First there were 12 children on the ride. Then 4 got off. Now there are 8 children on the ride.</p> 	 <p><math>12 - 4 =</math> <math>12 - 2 = 10</math> <math>10 - 2 = 8</math></p>
<p>There are more ___ than ___.</p> <p>There are fewer ___ than ___.</p> <p>The difference between ___ and ___ is ___.</p> <p><b>Year 2</b></p>	 <p>The difference between 2 and 5 is 3. The difference between 5 and 2 is 3.</p>	 <p>The difference between 4 and 7 is 3. The difference between 7 and 4 is 3.</p>	 <p>5 red cars 3 blue cars</p> <p><math>5 - 3 = 2</math></p>

<p>I know that <u>  </u> minus <u>  </u> is equal to <u>  </u>. (single-digit fact)</p> <p>So <u>  </u> minus <u>  </u> is equal to <u>  </u>. (related two-digit minus single digit fact)</p> <p>I know that ten minus <u>  </u> is equal to <u>  </u> so <u>  </u> minus <u>  </u> is equal to <u>  </u>.</p> <p><b>Year 2</b></p>	 <p><math>7 - 3 = 4</math> <math>47 - 3 = 44</math></p> <p><math>20 - 3 = 17</math></p>	 <p><math>9 - 3 = 6</math> <math>99 - 3 = 96</math></p>	 <p><math>47 - 3 = 44</math></p>
<p>I know that <u>  </u> minus <u>  </u> is equal to <u>  </u>. So <u>  </u> tens minus <u>  </u> tens is equal to <u>  </u> tens.</p> <p><b>Year 2</b></p>	 <p><math>70 - 30 = 40</math> so <math>75 - 30 = 45</math></p>	 <p><math>75 - 30 = 45</math></p>	 <p><math>5 - 3 = 2</math> <math>5 \text{ tens} - 3 \text{ tens} = 2 \text{ tens}</math> <math>50 - 30 = 20</math></p>
<p>First I subtract the tens, then I subtract the ones.</p> <p><b>Year 2</b></p>	 <p><math>45 - 23 =</math> <math>45 - 20 = 25</math> <math>25 - 3 = 22</math></p>	<p><math>67 - 34 = 33</math></p> 	<p><math>45 - 23 = 22</math></p>
<p>First I subtract the tens, then I subtract the ones.</p> <p><b>Year 2</b></p>		 <p><math>62 - 34 = 28</math></p> 	<p><math>63 - 17 = 46</math></p>

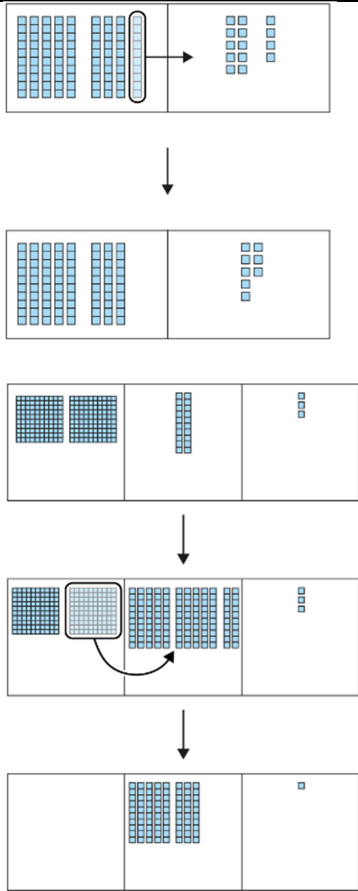
<p>I know that ___ minus ___ is equal to ___. (bridging ten)</p> <p>So ___ tens minus ___ tens is equal to ___ tens. (bridging ten tens)</p> <p>One hundred and ___ minus ___ is equal to ___.</p> <p><b>Year 3</b></p>	<p>See Year 2 (bridging)</p>  <p><math>126 - 70 = 56</math></p>	 <p><math>120 - 30 =</math>  <math>120 - 20 = 100</math>  <math>100 - 10 = 90</math></p>	 <p><math>120 - 30 = 90</math></p> <p><math>120 - 30 =</math>  <math>120 - 20 = 100</math>  <math>100 - 10 = 90</math></p>
<p>I know that ___ minus ___ is equal to ___. (bridging ten)</p> <p>So ___ tens minus ___ tens is equal to ___ tens. (bridging ten tens)</p> <p>One hundred and ___ minus ___ is equal to ___.</p> <p><b>Year 3</b></p>	 <p><math>126 - 70 = 56</math></p>	 <p><math>126 - 70 = 56</math></p>	 <p><math>126 - 70 = 56</math></p> <p><math>126 - 70 = 120 - 70 + 6</math>  <math>= 50 + 6</math>  <math>= 56</math></p>
<p>We partition the ___ into ___ and ___. First we subtract the ___ from ___ to get to a multiple of 10. Then we subtract the remaining ___ from the multiple of 10. We know 10 minus ___ is equal to ___ so ___ minus ___ is equal to ___.</p> <p><b>Year 3</b></p>		<p><math>544 - 16</math></p> 	<p>Count back to multiples of 10/100</p>
<p>We partition the ___ into ___ and ___. First we add the ___ to ___ to get to 100. Then we add the remaining ___ to 100. We know 100 plus ___ is equal to ___.</p> <p><b>Year 3</b></p>		 <p><math>123 - 97 = 26</math></p>	<p>Count on to multiples of 10/100</p>

We line up the ones; \_\_\_ ones plus \_\_\_ ones.  
 We line up the tens: \_\_\_ tens plus \_\_\_ tens.  
 The \_\_\_ is in the ones column – it represents \_\_\_ ones.  
 \_\_\_ ones minus \_\_\_ ones is equal to \_\_\_ ones.  
 The \_\_\_ is in the tens column – it represents \_\_\_ tens.  
 \_\_\_ tens minus \_\_\_ tens is equal to \_\_\_ tens.  
 In column subtraction we start at the right-hand side.



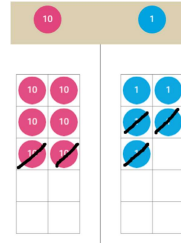
**Year 3**

If there is an insufficient number to subtract from in a given column, we must exchange from the column to the left.

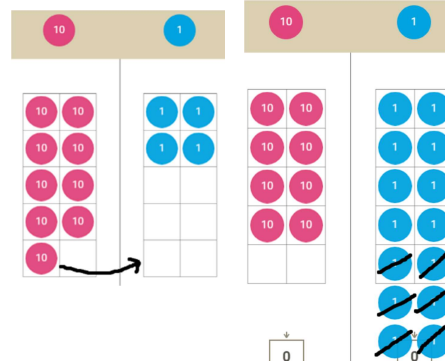


**Year 3**

Children could draw place value counters.



Children could draw place value counters.



$$\begin{array}{r} 65 \\ - 23 \\ \hline 42 \end{array}$$
  

$$\begin{array}{r} 462 \\ - 251 \\ \hline \end{array}$$

10s	1s
<del>9</del> <sup>8</sup>	14
-	6

10s	1s
<del>9</del> <sup>8</sup>	14
-	6
8	8

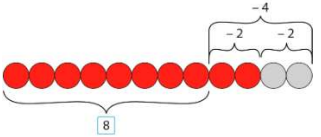
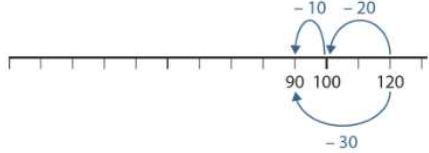
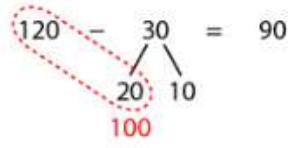
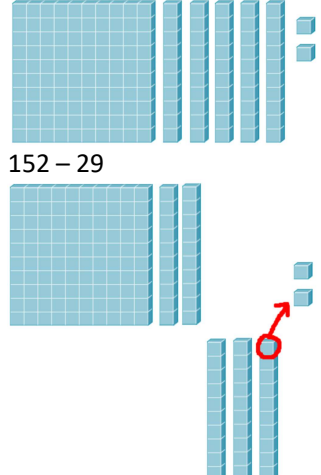
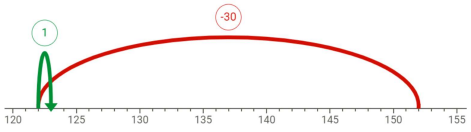
100s	10s	1s
2	2	3
-	1	4

100s	10s	1s
<del>2</del> <sup>1</sup>	12	3
-	1	4

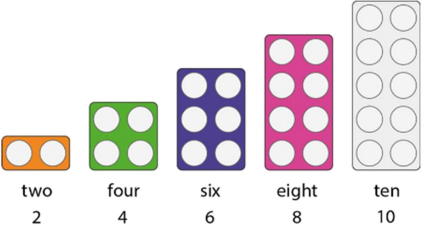
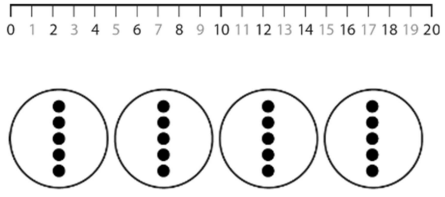


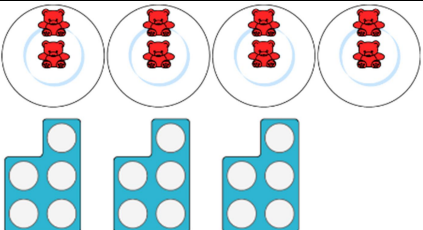
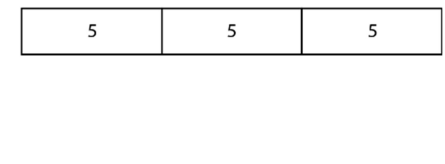

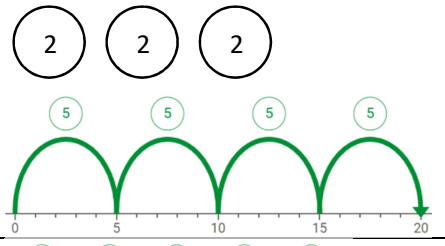
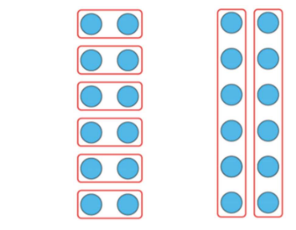
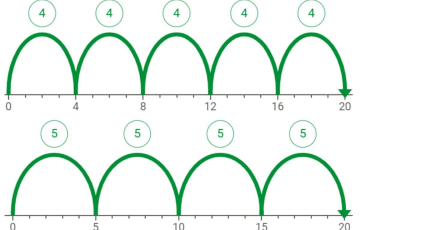
100s	10s	1s
<del>2</del> <sup>1</sup>	12	3
-	1	4
0	8	1

<p>If there is an insufficient number to subtract from in a given column, we must exchange from the column to the left.</p> <p><b>Year 4</b></p>	<p>See Year 3 examples</p>	<p>See Year 3 examples</p>	$\begin{array}{r} \overset{\cancel{5}}{6}, \overset{\cancel{4}}{5}, \overset{\cancel{2}}{3}, \overset{\cancel{1}}{8} \\ - 2, 7, 8, 9 \\ \hline 3, 7, 4, 9 \end{array}$ $\begin{array}{r} \pounds 2, \overset{\cancel{8}}{9}, \overset{\cancel{14}}{5}, \overset{\cancel{1}}{0} \\ - \pounds 1, 8, 9, 4 \\ \hline \pounds 1, 0, 5, 6 \end{array}$
<p>If there is an insufficient number to subtract from in a given column, we must exchange from the column to the left.</p> <p><b>Years 5 and 6</b></p>	<p>See Year 3 examples</p>	<p>See Year 3 examples</p>	<p>As in Year 4 but using numbers with more than 4 digits</p>

## Subtraction – Key mental strategies for Key Stage 2

Strategy	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
Bridging through a multiple of 10, 100, etc  <b>Years 3, 4, 5 and 6</b>	 $12 - 4 =$ $12 - 2 = 10$ $10 - 2 = 8$ $\begin{array}{r} 12 \\ - 4 \\ \hline 2 \quad 2 \end{array}$	 $120 - 30 =$ $120 - 20 = 100$ $100 - 10 = 90$	 $120 - 30 =$ $120 - 20 = 100$ $100 - 10 = 90$
Compensating – rounding to the nearest multiple 10, 100, etc and adjusting  <b>Years 3, 4, 5 and 6</b>	 $152 - 29$		$152 - 30 = 122$ $122 + 1 = 123$

## Multiplication

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>One group of two, two groups of two, three groups of 2, ...</p> <p>Ten, twenty, thirty, ...</p> <p>One five, two fives, three fives, ...</p> <p><b>Year R/1</b></p>	 <p style="text-align: center;">two      four      six      eight      ten 2            4            6            8            10</p>		<p>10, 20, 30, ...</p>
<p>There are __ coins.</p> <p>Each coin has a value of __p.</p> <p>This is __p.</p> <p><b>Year 1</b></p>	 <p style="text-align: center;">Representing each group by one object</p>		<p>Five 2p coins = 10p</p>
<p>There are __ in each group.</p> <p>There are __ groups.</p> <p>There are __ in a group and __ groups.</p> <p><b>Year 2</b></p>			<p><math>2 + 2 + 2 + 2 = 8</math></p> <p><math>2 \times 4 = 8</math></p> <p><math>5 + 5 + 5 = 15</math></p> <p><math>5 \times 3 = 15</math></p>
<p>Factor times factor is equal to the product.</p> <p>The product is equal to factor times factor.</p> <p><b>Year 2</b></p>	 <p style="text-align: center;">Unitising equal groups – representing each group by one object</p>		<p><math>2 \times 3 = 6</math></p> <p><math>6 = 2 \times 3</math></p>
<p>__ times __ can represent __ in a group and __ groups.</p> <p>It can also represent __ groups of __.</p> <p>Multiplication is commutative.</p> <p><b>Year 2</b></p>			<p><math>2 \times 5 = 5 \times 2</math></p>



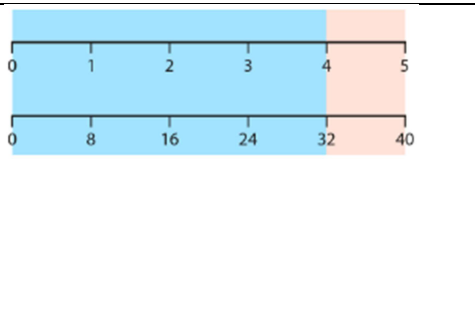
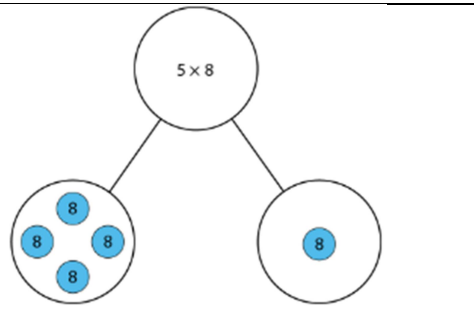
\_\_ is equal to \_\_ plus \_\_, so \_\_ times \_\_ is equal to \_\_ times \_\_ plus \_\_ times \_\_.

\_\_ is equal to \_\_ minus \_\_, so \_\_ times \_\_ is equal to \_\_ times \_\_ minus \_\_ times \_\_.

Multiplication is distributive.

(NCETM Year 4 unit 2.10)

**Year 3**



$$5 = 4 + 1$$

$$5 \times 8 = 4 \times 8 + 1 \times 8$$

$$= 32 + 8$$

$$= 40$$
  

$$4 = 5 - 1$$

$$4 \times 8 = 5 \times 8 - 1 \times 8$$

$$= 40 - 8$$

$$= 32$$

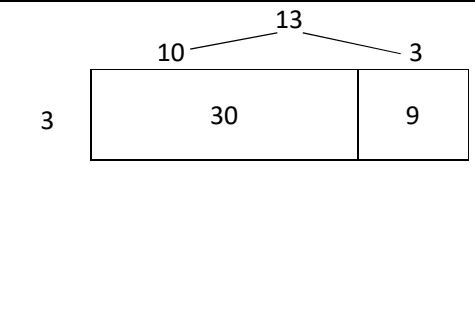
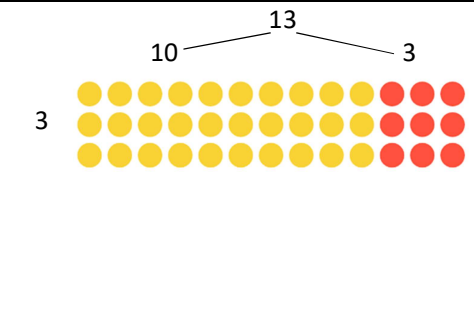
\_\_ is equal to \_\_ plus \_\_, so \_\_ times \_\_ is equal to \_\_ times \_\_ plus \_\_ times \_\_.

\_\_ is equal to \_\_ minus \_\_, so \_\_ times \_\_ is equal to \_\_ times \_\_ minus \_\_ times \_\_.

Multiplication is distributive.

(NCETM Year 4 unit 2.10)

**Year 3**



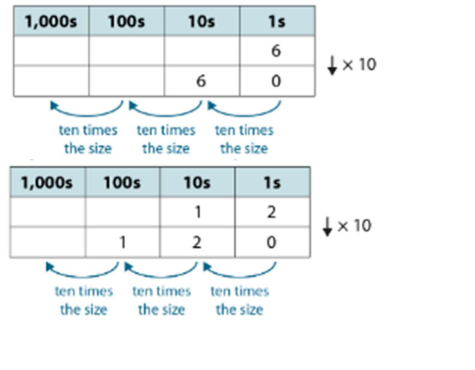
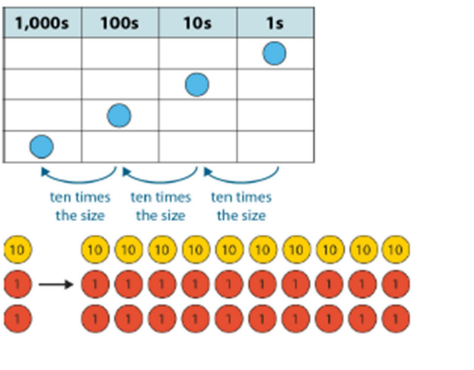
$$3 \times 13 = 3 \times 10 + 3 \times 3$$

$$= 30 + 9$$

$$= 39$$

To multiply a whole number by 10, place a zero after the final digit of that number.

**Year 4**

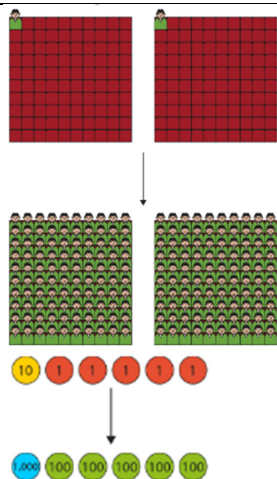


$$6 \times 10 = 60$$
  

$$12 \times 10 = 120$$

All multiples of 100 have both a tens and ones digit of 0.  
 When a number is multiplied by 100, the product is a multiple of 100.

**Year 4**



1,000s	100s	10s	1s
	6	0	0

↓ × 100

100 times the size

1,000s	100s	10s	1s
1	5	0	0

↓ × 100

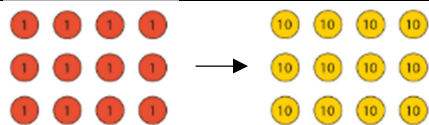
100 times the size    100 times the size

$2 \times 100 = 200$   
 There are 100 times as many people as before.

$15 \times 100 = 1500$

If one factor is made ten times the size, the product will be ten times the size.

**Year 4**



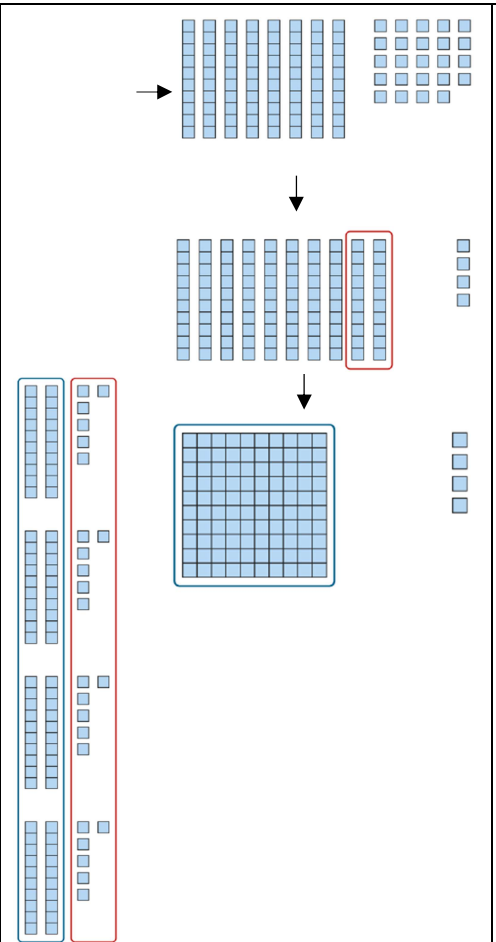
$$\begin{array}{r}
 2 \times 3 = 6 \\
 \times 10 \quad \downarrow \times 10 \\
 2 \times 30 = 60
 \end{array}$$

$4 \times 3 = 12$  so  $4 \times 30 = 120$

If there are ten or more ones, we must regroup the ones into tens and ones.  
 If there are ten or more tens, we must regroup the tens into hundreds and tens.

Multiplication is distributive.

**Year 4**



$$84 \times 6 = 504$$

$$\begin{array}{r} 84 \\ 80 \quad 4 \end{array}$$

$$80 \times 6 = 480$$

$$4 \times 6 = 24$$

$$480 + 24 = 504$$

$$84 \times 6 = 80 \times 6 + 4 \times 6$$

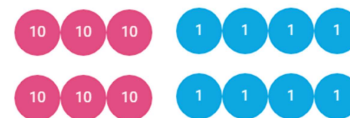
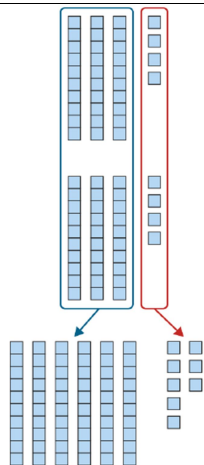
$$= 480 + 24$$

$$= 504$$

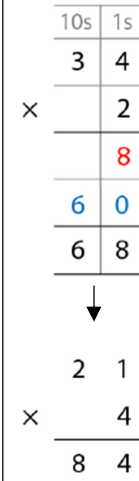
We work from the least significant digit, on the right, to the most significant digit, on the left.

Multiplication is distributive.

**Year 4**



$$34 \times 2 = 60 + 8 = 68$$



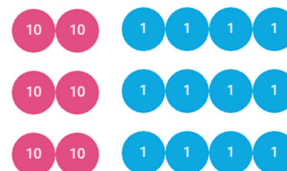
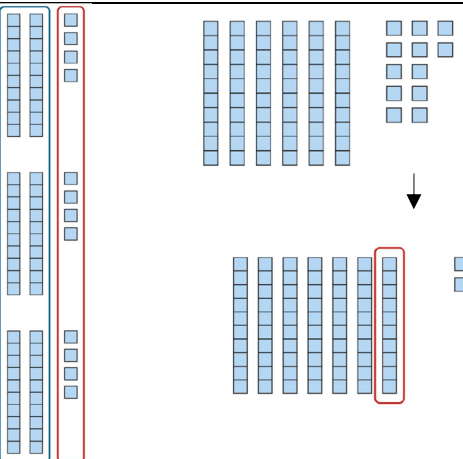
$2 \times 4 \text{ ones} = 8 \text{ ones}$

$2 \times 3 \text{ tens} = 6 \text{ tens}$

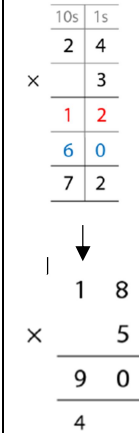
If there are ten or more ones, we must regroup the ones into tens and ones.  
If there are ten or more tens, we must regroup the tens into hundreds and tens.

Multiplication is distributive.

**Year 4**

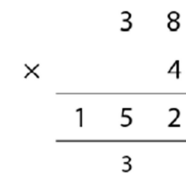


$$24 \times 3 = 60 + 12 = 72$$



$3 \times 4 \text{ ones} = 12 \text{ ones} = 1 \text{ ten} + 2 \text{ ones}$

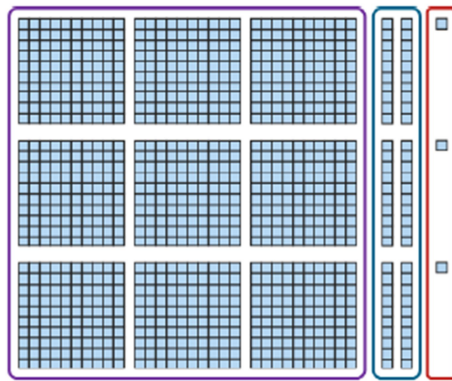
$3 \times 2 \text{ tens} = 6 \text{ tens}$



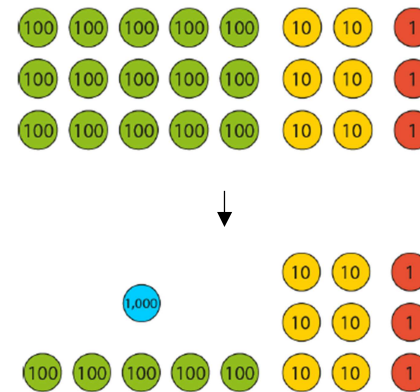
If there are ten or more ones, we must regroup the ones into tens and ones.  
 If there are ten or more tens, we must regroup the tens into hundreds and tens.  
 If there are ten or more hundreds, we must regroup the hundreds into thousands and hundred.

Multiplication is distributive.

**Year 4**



$$321 \times 3 = 963$$



$$521 \times 3 = 1000 + 500 + 60 + 3 = 1563$$

100s	10s	1s
3	2	1
×		
3		
3		
6	0	
9	0	0
9	6	3
×		
3		
3		
3	2	1
×		
3		
3		
9	6	3

$3 \times 1 \text{ ones} = 3 \text{ ones}$   
 $3 \times 2 \text{ tens} = 6$   
 $3 \times 3 \text{ hundred}$

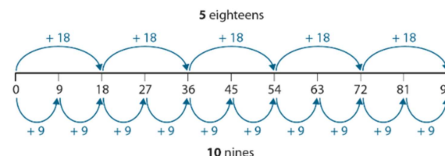
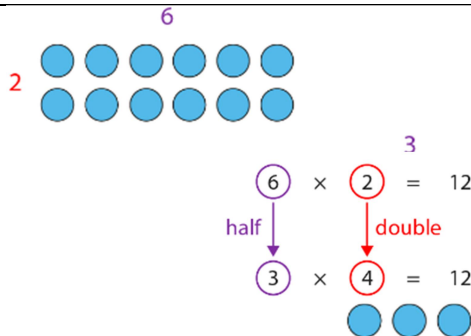
1,000s	100s	10s	1s
	5	2	1
×			
3			
3			
		6	0
1	5	0	0
×			
3			
3			
		6	0
1	5	6	3

	3	6	7
×			
4			
1	4	6	8
×			
2			
2	2		

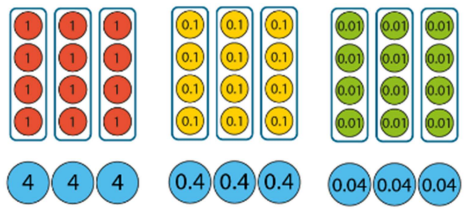
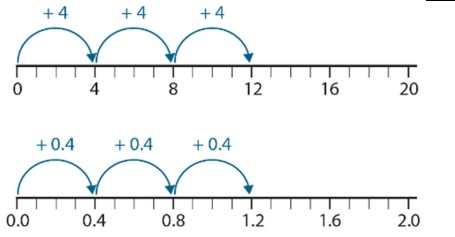
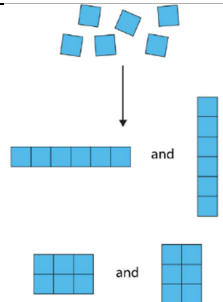
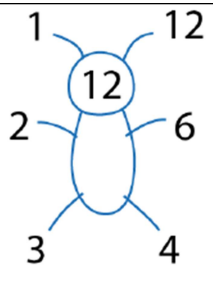
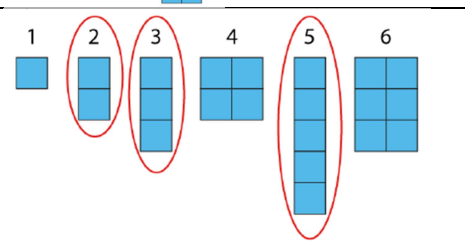
If there is a multiplicative increase in one factor and a multiplicative decrease in the other, the product remains the same.

If I multiply one factor by \_\_, I must divide the other factor by \_\_ for the product to remain the same.

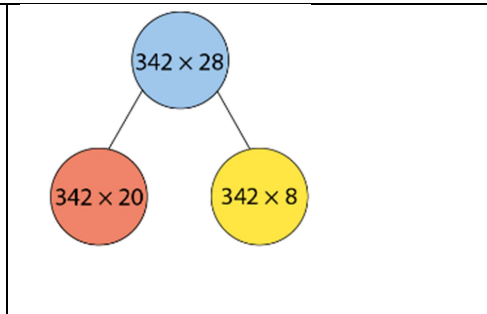
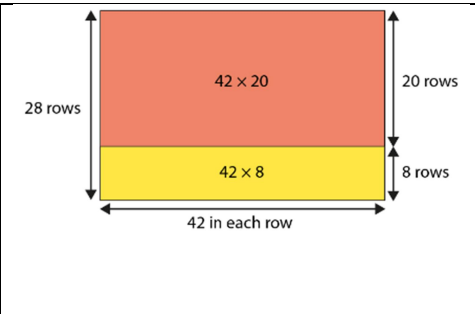
**Year 5 and 6**



$$\begin{matrix} 2 \\ \times 3 \\ \hline 6 \end{matrix} \times \begin{matrix} 9 \\ \div 3 \\ \hline 3 \end{matrix} = 18$$

<p>If one factor is made one tenth of the size, the product will be one tenth of the size.</p> <p>If one factor is made one hundredth of the size, the product will be one hundredth of the size.</p> <p>I move the digits of the number I am multiplying __ places to the left until I get a whole number; then I multiply; then I move the digits of the product __ places to the right.</p> <p><b>Year 5</b></p>	 <p>4 × 3 = 12 0.4 × 3 = 1.2 0.04 × 3 = 0.12</p>		$\begin{array}{r} 456 \\ \times \quad 4 \\ \hline 1824 \\ \phantom{1}22 \\ \hline \end{array}$ $\begin{array}{r} 4.56 \\ \times \quad 4 \\ \hline 18.24 \\ \phantom{1}22 \\ \hline \end{array}$
<p>Numbers that have more than two factors are composite numbers.</p> <p><b>Year 5</b></p>	 <p>Factors of 6 are 1, 2, 3 and 6.</p>	 <p>Factor bugs</p>	<p>Factors of 6 are 1, 2, 3 and 6.</p>
<p>Numbers that have only two factors are prime numbers.</p> <p><b>Year 5</b></p>			<p>17 is a prime number because its only factors are 1 and 17.</p>

To multiply two two-digit numbers, first multiply by the ones, then multiply by the tens, then add them together.  
 To multiply a three-digit number by a two-digit number, first multiply by the ones, then multiply by the tens, then add them together.



	100s	10s	1s
27		2	7
× 3		2	3
<hr/>			
	8	1	
27 × 3			
27 × 20	5	4	0
	6	2	1
			1

		3	1	2
×			2	8
<hr/>				
	2	4	9	6
<hr/>				
	6	2	4	0
<hr/>				
	8	7	3	6
<hr/>				
				1

**Year 6**





## Multiplication – Key mental strategies for Key Stage 2

Strategy	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
Adjacent multiples of ___ have a difference of ___.  <b>Year 3 onwards</b>			$4 \times 6 = 4 \times 5 + 4$  $4 \times 9 = 4 \times 10 - 4$
Products in the 10 times table are double the products in the 5 times table. Products in the 5 times table are half of the products in the 10 times table.  (NCETM Year 2 unit 2.5) <b>Year 3 onwards</b>			$5 \times 4 = 10 \times 2$
Products in the 4 times table are double the products in the 2 times table. Products in the 2 times table are half of the products in the 4 times table.  <b>Year 3 onwards</b>			$2 \times 6 = 4 \times 3$
Products in the 8 times table are double the products in the 4 times table. Products in the 4 times table are half of the products in the 8 times table.  <b>Year 3 onwards</b>			$4 \times 6 = 8 \times 3$
Products in the 6 times table are double the products in the 3 times table. Products in the 3 times table are half of the products in the 6 times table.  <b>Year 3 onwards</b>			$3 \times 4 = 6 \times 2$



When both factors are odd, the product is odd.  
 When one factor is odd and the other factor is even, the product is even.

(NCETM Year 3 unit 2.9)  
**Year 3 onwards**

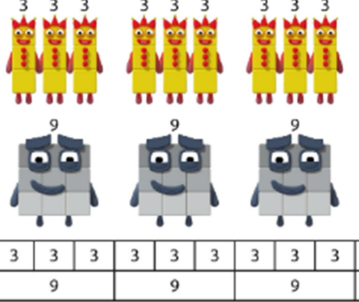
	$1 \times 7 = 7$	$7 \times 1 = 7$
odd	odd	odd
	$2 \times 7 = 14$	$7 \times 2 = 14$
even	odd	even
	$3 \times 7 = 21$	$7 \times 3 = 21$
odd	odd	odd
	$4 \times 7 = 28$	$7 \times 4 = 28$
even	odd	even

odd x odd = odd  
 odd x even = even  
 even x odd = even  
 even x even = even

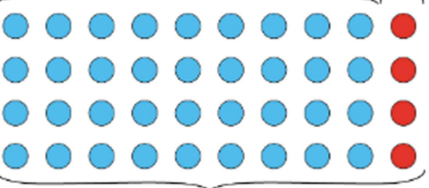
Products in the 9 times table are triple the products in the 3 times table.

Products in the 10 times table can be used to find products in the 9 times table.


(NCETM Year 3 unit 2.8)  
**Year 4 onwards**



$9 \times 4$                        $1 \times 4$



$10 \times 4$

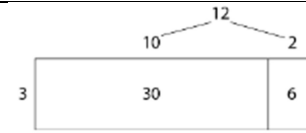
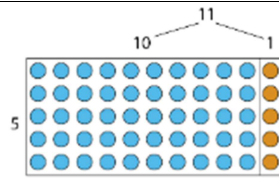


$3 \times 12 = 9 \times 4$

$9 \times 4 = 10 \times 4 - 1 \times 4$


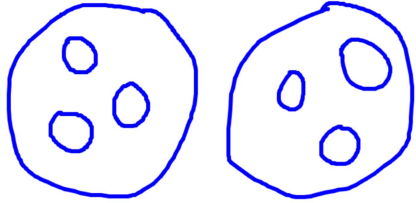

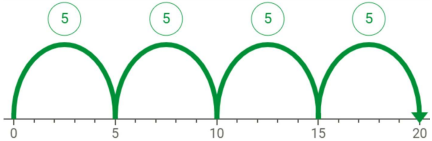

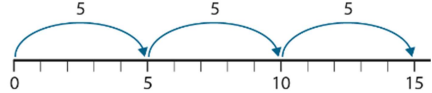
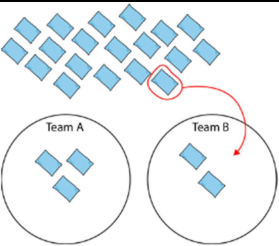
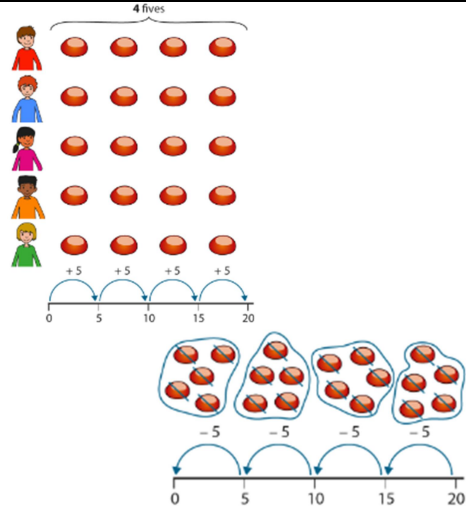
Products in the 10 times table can be used to find products in the 11 times table and 12 times table.

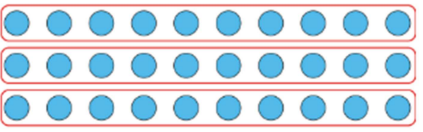
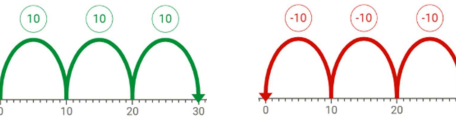
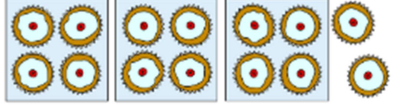
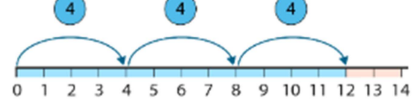
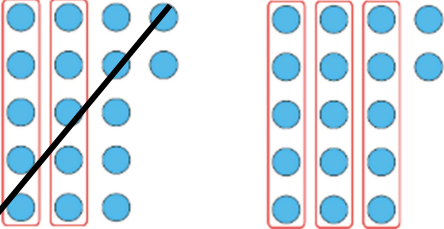
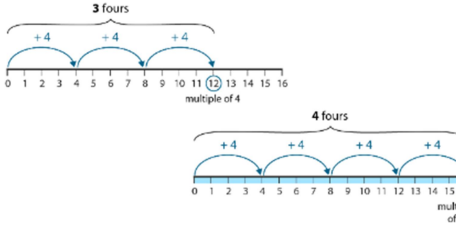
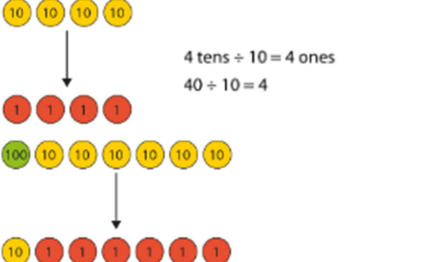
**Year 4 onwards**



$$\begin{aligned} 12 \times 3 &= 10 \times 3 + 2 \times 3 \\ &= 30 + 6 \\ &= 36 \end{aligned}$$

## Division

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>One group of two, two groups of two, three groups of 2, ...</p> <p>Ten, twenty, thirty, ...</p> <p>One five, two fives, three fives, ...</p> <p><b>Year R/1</b></p>			<p>6 biscuits shared between 2 children gives 3 biscuits each.</p>
<p>The _____ costs __p.</p> <p>Each coin has a value of __p.</p> <p>So I need __ coins.</p> <p><b>Year 1</b></p>			<p>Five 2p coins = 10p</p>
<p>__ is divided into groups of __.</p> <p>There are __ groups.</p> <p>We can skip count using the divisor to find the quotient.</p> <p><b>Year 2</b></p>			<p><math>5 + 5 + 5 = 15</math></p> <p><math>15 \div 5 = 3</math></p>
<p>__ divided between __ is equal to __ each.</p> <p>We can skip count using the divisor to find the quotient.</p> <p><b>Year 2</b></p>			<p>One 5 is 1 each. That's 5.</p> <p>Two 5s is 2 each. That's 10.</p> <p><math>10 \div 5 = 2</math></p>

<p>Ten times <u>  </u> is equal to <u>  </u> so <u>  </u> divided into groups of ten is <u>  </u>. If the divisor is <u>  </u>, we can use the <u>  </u> times table to find the quotient.</p> <p><b>Year 2</b></p>	 <p>30 represents the total number of counters. 10 represents the number in each group. 3 represents the number of groups.</p>		$10 \times 3 = 30$ $3 \times 10 = 30$ $30 \div 10 = 3$												
<p><u>  </u> is divided into groups of <u>  </u>. There are <u>  </u> groups and a remainder of <u>  </u>.</p> <p>(NCETM Year 4 unit 2.12)</p> <p><b>Year 3</b></p>			$14 = 4 \times 3 + 2$ $14 \div 4 = 3 \text{ r } 2$												
<p><u>  </u> is a multiple of <u>  </u> so when it is divided into groups of <u>  </u>, there is no remainder.</p> <p>The remainder is always less than the divisor.</p> <p>(NCETM Year 4 unit 2.12)</p> <p><b>Year 3 or 4?</b></p>			$17 \div 5 = 2 \text{ r } 7$ is incorrect because 7 is greater than 5.  $17 \div 5 = 3 \text{ r } 2$												
<p>To divide a multiple of ten by 10, remove the zero from the ones place.</p> <p><b>Year 4</b></p>	 <p><math>4 \text{ tens} \div 10 = 4 \text{ ones}</math>  <math>40 \div 10 = 4</math></p>	<table border="1" data-bbox="1102 901 1407 990"> <thead> <tr> <th>1,000s</th> <th>100s</th> <th>10s</th> <th>1s</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td>9</td> <td>0</td> </tr> <tr> <td></td> <td></td> <td></td> <td>9</td> </tr> </tbody> </table> <p><math>\downarrow \div 10</math></p> <p><math>\times 10</math>   <math>\times 10</math>   <math>\times 10</math>  ten times the size   ten times the size   ten times the size</p>	1,000s	100s	10s	1s			9	0				9	$90 \div 10 = 9$  $150 \div 10 = 15$
1,000s	100s	10s	1s												
		9	0												
			9												

To divide a multiple of 100 by 100, remove two zeros (from the tens and ones places).

Year 4

100 times as many

$\times 100$

$\square \times 100 = 200$        $200 \div 100 = \square$

1,000s	100s	10s	1s
	9	0	0
			9

↓ + 100      0      0

100 times the size      100 times the size

$900 \div 100 = 9$

$1500 \div 100 = 15$

If the dividend is made ten times the size, the quotient will be ten times the size.

Year 4

$8 \div 4 = 2$

$80 \div 4 = 20$

$12 + 3 = 4$

$\times 10$

$120 + 3 = 40$

If dividing the tens gives a remainder of one or more tens, we must exchange the remaining tens for ones.

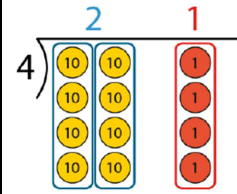
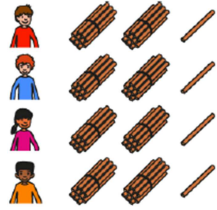
Year 4

$84 \div 4 = 21$

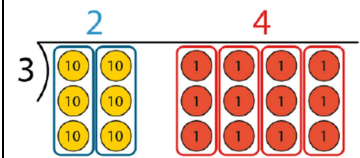
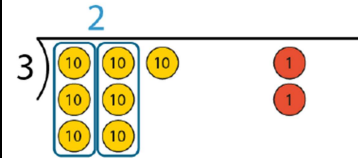
8 tens	÷	4	=	2 tens
4 ones	÷	4	=	1 one
<hr/>				
84	÷	4	=	21
 ↓				
6 tens	÷	3	=	2 tens
21 ones	÷	3	=	7 ones
<hr/>				
81	÷	3	=	27

If dividing the tens gives a remainder of one or more tens, we must exchange the remaining tens for ones.

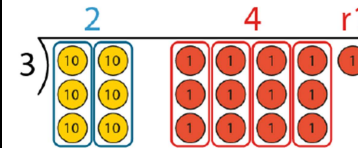
Year 4



$$72 \div 4 = 18$$



$$73 \div 3 = 24 \text{ r } 1$$



$$\begin{array}{r} \text{10s} \quad \text{1s} \\ 4 \overline{) 21} \\ \underline{8} \quad 4 \\ 4 \end{array}$$

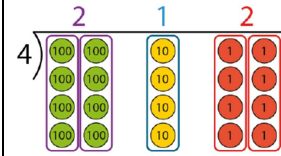
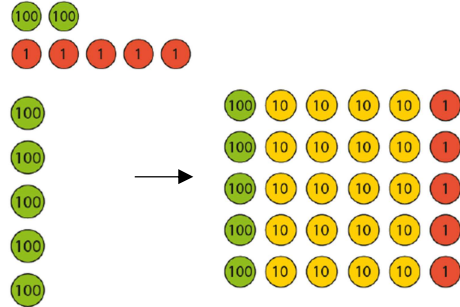
8 tens  $\div$  4 = 2 tens  
4 ones  $\div$  4 = 1 one

$$\begin{array}{r} 2 \quad 4 \\ 3 \overline{) 71} \\ \underline{7} \quad 1 \\ 2 \end{array}$$

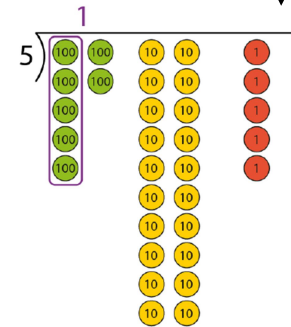
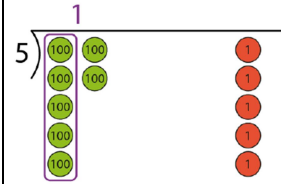
$$\begin{array}{r} 2 \quad 4 \text{ r } 1 \\ 3 \overline{) 73} \\ \underline{7} \quad 3 \\ 1 \end{array}$$

If dividing the hundreds gives a remainder of one or more hundreds, we must exchange the remaining hundreds for tens.

Year 4

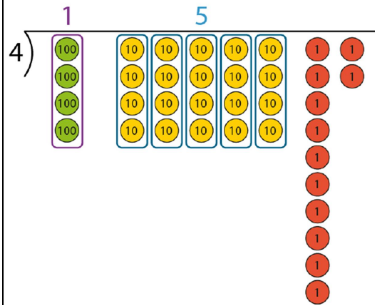
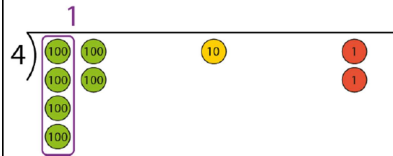


$$\begin{array}{r} 212 \\ 4 \overline{) 612} \end{array}$$



$$\begin{array}{r} 141 \\ 5 \overline{) 705} \end{array}$$

$$612 \div 4 = 153$$



$$\begin{array}{r} 153 \\ 4 \overline{) 612} \end{array}$$

If there is a multiplicative change to the dividend factor and a corresponding change to the divisor, the quotient remains the same.

If I multiply the dividend by \_\_, I must multiply the divisor by \_\_ for the quotient to remain the same.

**Year 5 and 6**

$3 \div 1 = 3$   
 $\times 3 \quad \times 3$   
 $9 \div 3 = 3$

$40 \div 10 = 4$   
 $\times 10 \quad \times 10$   
 $400 \div 100 = 4$

If the dividend is made one tenth of the size, the quotient will be one tenth of the size.

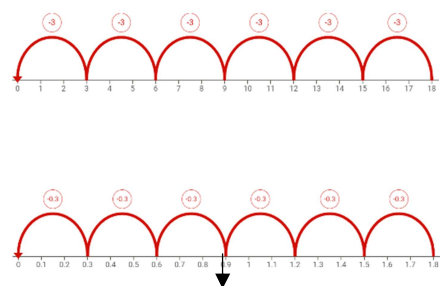
If the dividend is made one hundredth of the size, the quotient will be one hundredth of the size.

I move the digits of the dividend \_\_ places to the left until I get a whole number; then I divide; then I move the digits of the quotient \_\_ places to the right.

**Year 5 onwards**

$2 \overline{) 12}$

$2 \overline{) 1.2}$



$0.85 \div 5 =$

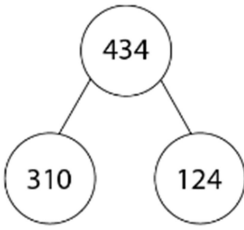
$85 \div 5 = 17$

$0.17$



Any two-, three- or four-digit dividend can be divided by a two-digit divisor using skip-counting in multiples of the divisor, or by short division or long division.

Year 6

Partitioning	Short division	Long division
 $\begin{array}{r} 310 \div 31 = 10 \\ 124 \div 31 = 4 \\ \hline 434 \div 31 = 14 \end{array}$	$\begin{array}{r} 0 \quad 1 \quad 4 \\ 31 \overline{) 4 \quad 3 \quad 12 \quad 4} \end{array}$	$\begin{array}{r} 0 \quad 1 \quad 4 \\ 31 \overline{) 4 \quad 3 \quad 4} \\ \underline{3 \quad 1} \phantom{0} \\ 1 \quad 2 \quad 4 \\ \underline{1 \quad 2 \quad 4} \\ 0 \end{array}$ <p>(1 ten <math>\times</math> 31 = 31 tens) (4 ones <math>\times</math> 31 = 124 ones)</p>

Where there is a remainder, the result can be expressed as a whole-number quotient with a whole-number remainder, a whole-number quotient with a proper-fraction remainder, or as a decimal-fraction quotient.

Year 6

$354 \div 15 = ?$

$\begin{array}{r} 2 \quad 3 \quad r9 \\ 15 \overline{) 3 \quad 5 \quad 4} \\ \underline{3 \quad 0} \phantom{0} \\ 5 \quad 4 \\ \underline{4 \quad 5} \\ 9 \end{array}$	$\begin{array}{r} 2 \quad 3 \quad \frac{9}{15} \\ 15 \overline{) 3 \quad 5 \quad 4} \\ \underline{3 \quad 0} \phantom{0} \\ 5 \quad 4 \\ \underline{4 \quad 5} \\ 9 \end{array}$	$\begin{array}{r} 2 \quad 3 \quad . \quad 6 \\ 15 \overline{) 3 \quad 5 \quad 4 \quad . \quad 0} \\ \underline{3 \quad 0} \phantom{00} \\ 5 \quad 4 \\ \underline{4 \quad 5} \phantom{0} \\ 9 \quad 0 \\ \underline{9 \quad 0} \\ 0 \end{array}$
So, $354 \div 15 = 23 \text{ r } 9$	So, $354 \div 15 = 23 \frac{3}{5}$	So, $354 \div 15 = 23.6$